

DEB theory and stable isotope dynamics: exploring alternative ways

Sébastien Lefebvre, Marine Ballutaud, Carlos Martinez Del Rio, Laure Pecquerie

Characters....



Sébastien Lefebvre,



Marine Ballutaud,



Carlos Martinez Del Rio,

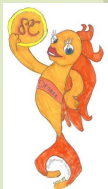


Laure Pecquerie

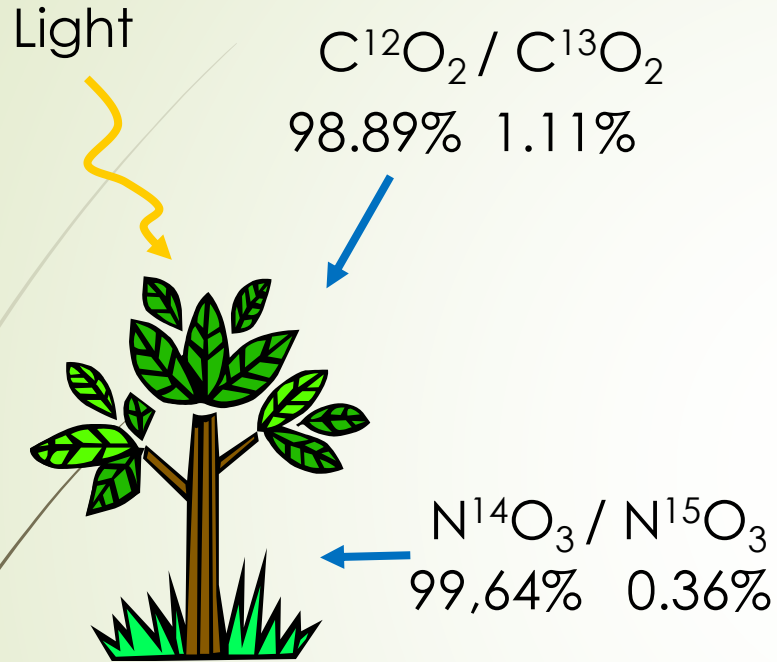


Debbie the special guest

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Introduction: basics on stable isotopes



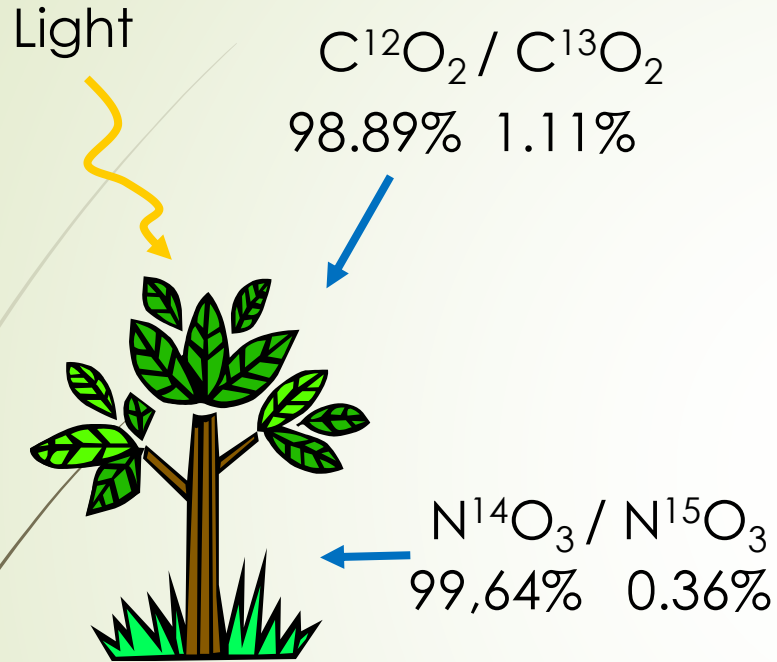
- Stable isotopes are twins with one extra neutron
- Usually the heavier is the rarer
- Carbon and nitrogen are the most used ones

^{12}C 12.00000 98.89% Stable	^{13}C 13.00335 1.11% Stable	^{14}C 14.0 $t_{1/2} = 5715\text{yrs}$ Radioactive Cosmogenic/ anthropogenic
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^{14}N 14.00307 99.63% Stable	^{15}N 15.0001 0.37% Stable
--	--



Introduction: basics on stable isotopes



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The delta (δ) notation

- Variations in proportion are very little (For ^{13}C : between 1.07 and 1.1 % !!)
- δ notation is a ratio (between sample and a reference/standard) of ratios (fraction of Heavy or Light isotopes)

$$\delta^H X = \left[\frac{R_{\text{sample}}}{R_{\text{standard}}} - 1 \right] * 1000 \quad R = \frac{F_H}{F_L}$$



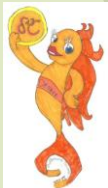
Introduction: basics on stable isotopes

You are what you eat (δ)

De Niro and Epstein, 1976



Diet
(& trophic position)



Introduction: basics on stable isotopes

You are what you eat (δ) + a few per mil (Δ)

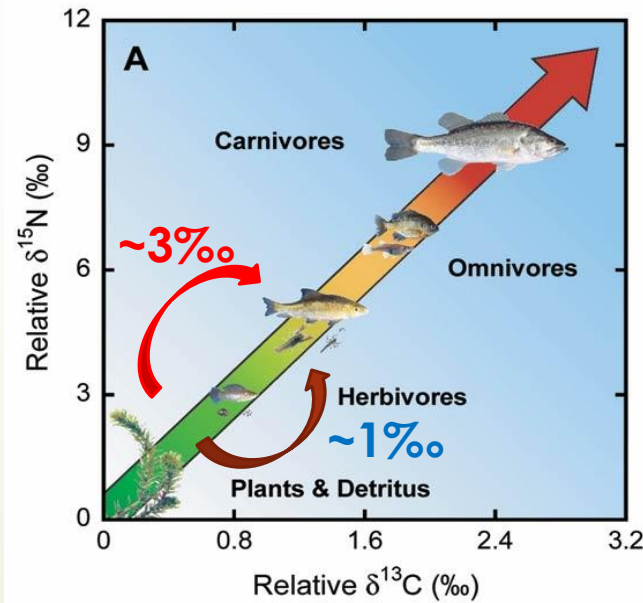
De Niro and Epstein, 1976

Diet
(& trophic position)

Discrimination factor
Excretion form
Diet quality and quantity...



Dual C, N isotopic plot



Introduction: basics on stable isotopes

You are what you eat (δ) + a few per mil (Δ) [+ time lag (λ)]

De Niro and Epstein, 1976

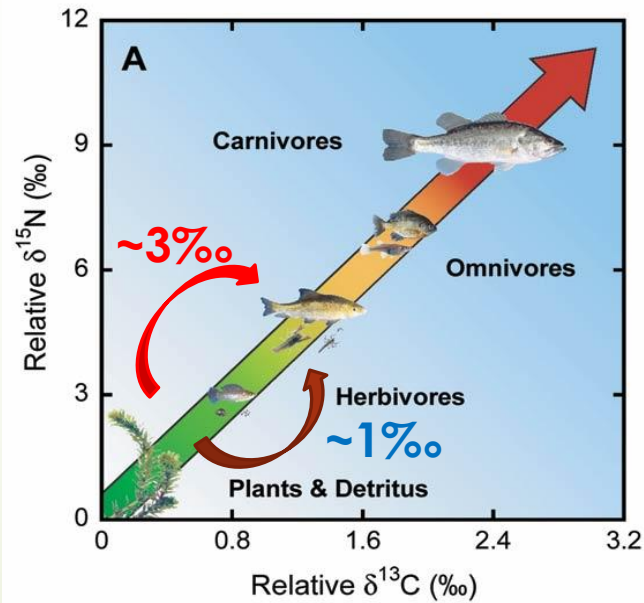
Diet
(& trophic position)

Discrimination factor
Excretion form
Diet quality and quantity...

Incorporation rate
Metabolic rate



Dual C, N isotopic plot



Introduction: basics on stable isotopes

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(& trophic position)

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Metabolic rate

Quantification of diet (or trophic position) is possible provided that:

- 1) Prey have different stable isotope ratios (or trophic baseline known)
- 2) The discrimination factor for each food source is known and constant
- 3) Isotopic equilibrium is reached



Introduction: basics on stable isotopes

You are what you eat (δ) + a few per mil (Δ) [+ time lag (λ)]

De Niro and Epstein, 1976

Diet
(& trophic position)

Discrimination factor
Excretion form
Diet quality and quantity...

Turnover rate
Metabolic rate

Quantification of diet (or trophic position) is possible provided that:

- 1) Prey have different stable isotope ratios (or trophic baseline known)
- 2) The discrimination factor for each food source is known and constant
- 3) Isotopic equilibrium is reached

Unlikely!
The tricky part.....



Burying our heads in the sand?

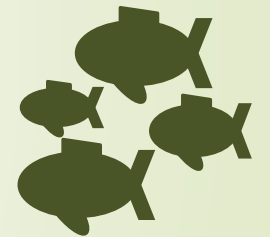


Introduction: basics on stable isotopes

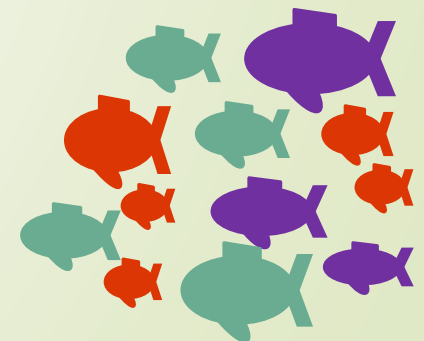
Level of organisation	Trophic inferences	Methods
Individual	Diet, Trophic position	Mixing models (Philipps and Gregs, 2003) Trophic position (Post 2002)
Population	Between and within individuals	Niche variation hypothesis, (Araujo et al., 2010)
Community	Structure of the food web	Isotope metrics (Layman et al., 2012)



individual



population



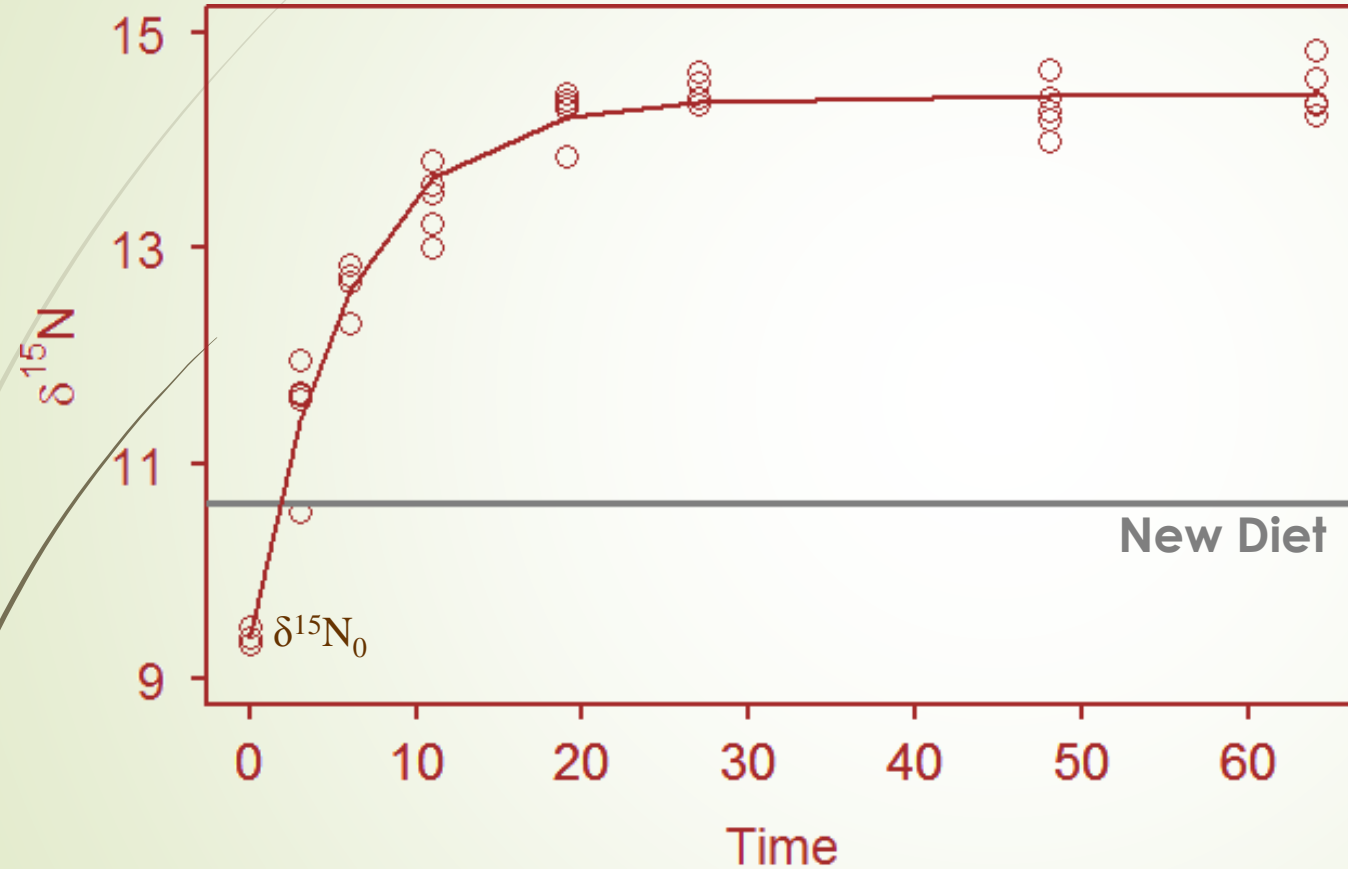
community

More than 600 papers a year (isotope* and trophic ISI WOS)



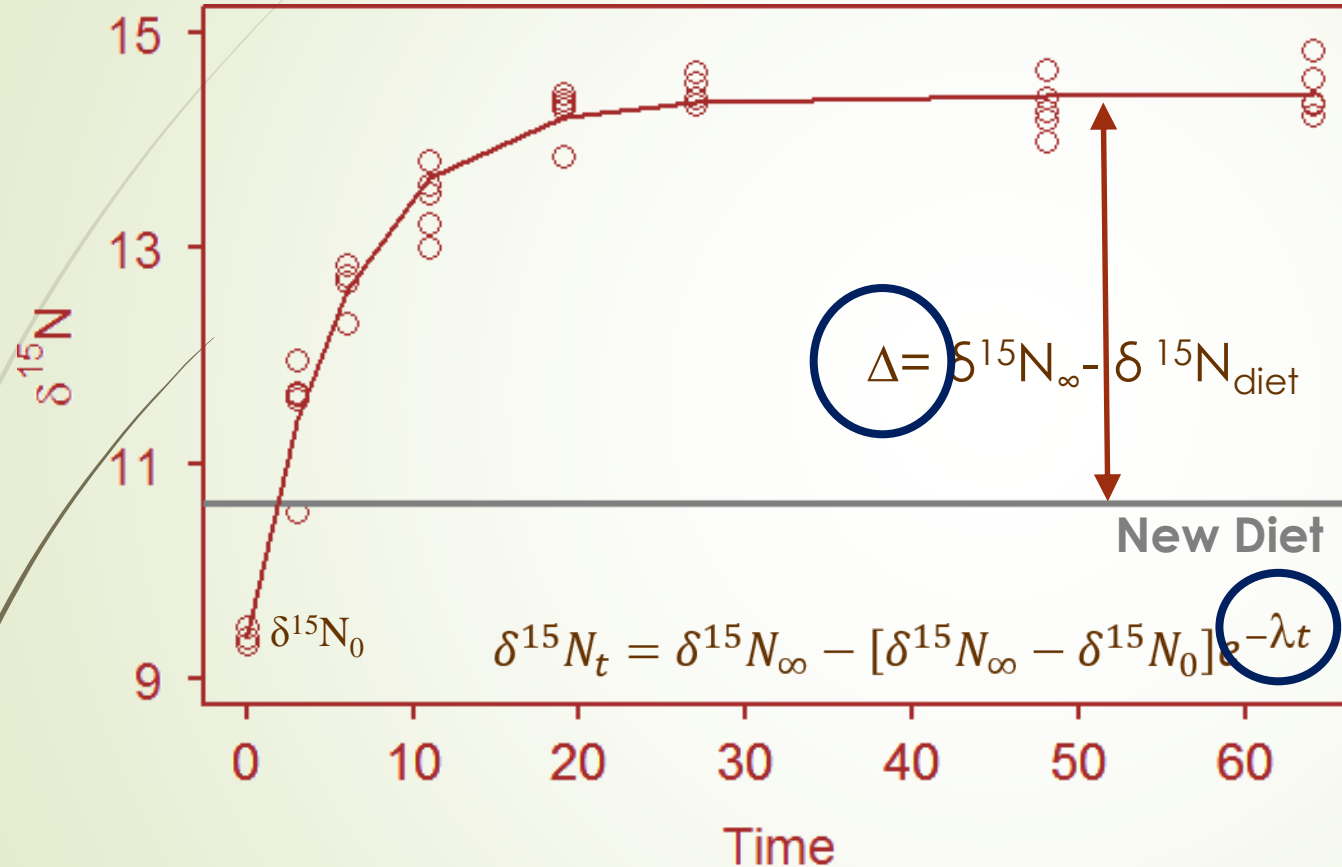
How to estimate discrimination and turnover

Diet Switch Experiments + « phenomenological » incorporation models



How to estimate discrimination and turnover

Diet Switch Experiments + « phenomenological » incorporation models



$$\lambda = \frac{1}{W} \frac{dW}{dt} - \alpha W^{\beta}$$

Turnover = growth term + catabolic term

Time- or growth-dependent models:

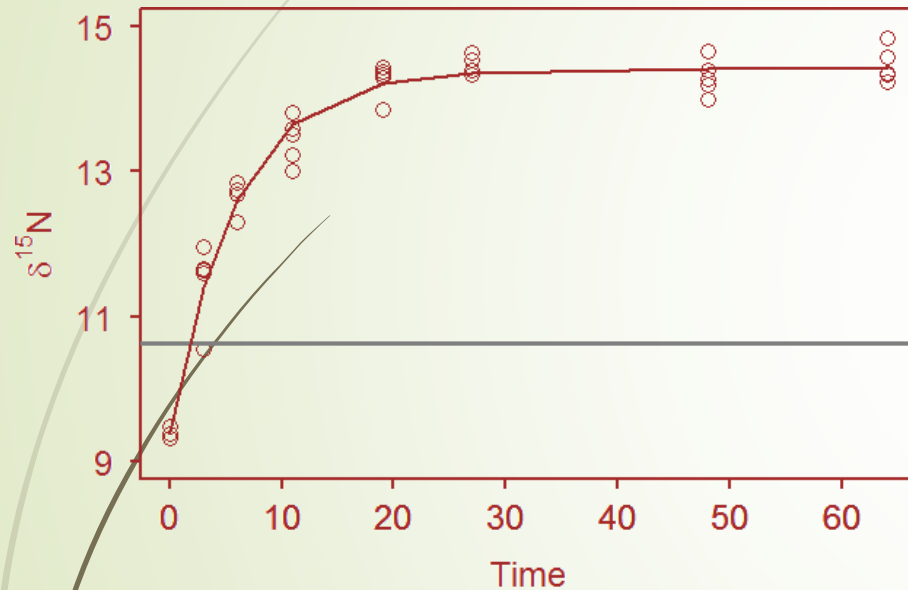
Fry and Arnold, 1982, Hobson et al., 1992,

Heisslein et al., 1993, Carleton & Martinez Del Rio, 2010



How to estimate discrimination and turnover

Diet Switch Experiments + « phenomenological » incorporation models



Few studies: Only 2% of experimental studies (on average 12 on 600 per year)

Isotopists then refer to meta-analyses and crude mean values for discrimination and turnover rate



Isotopic distorsion?

Diet = You are what you eat (δ) + a few per mil (Δ) + time lag (λ)

Sources of distorsion

Assuming mean Δ and high λ
→ distorsion



Distorted mirror

In reality, Δ and λ are dynamic and depend on several confounding factors of which metabolism

But few mechanistic rules were put in evidence

→ **Need for mechanistic modelling**

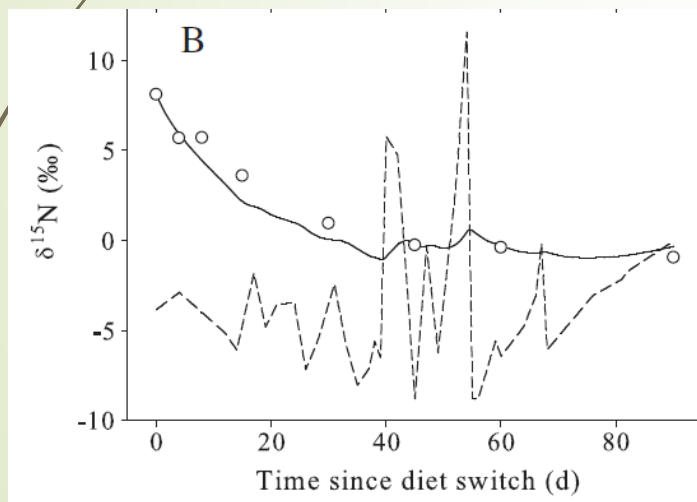


Mechanistic DIB modeling

2010

The impact of metabolism on stable isotope dynamics: a theoretical framework

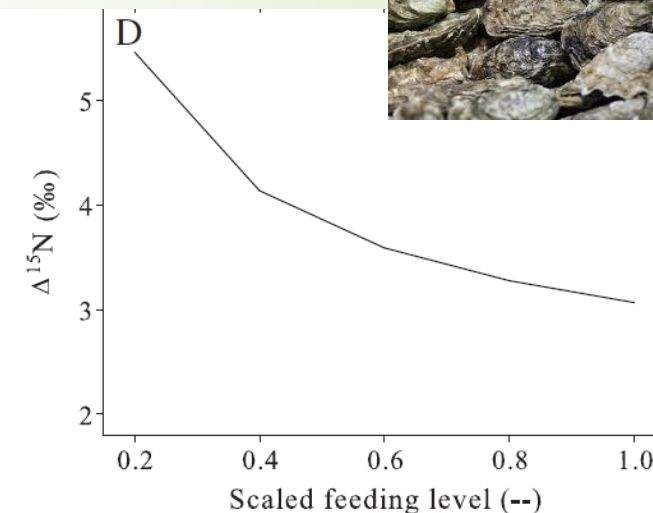
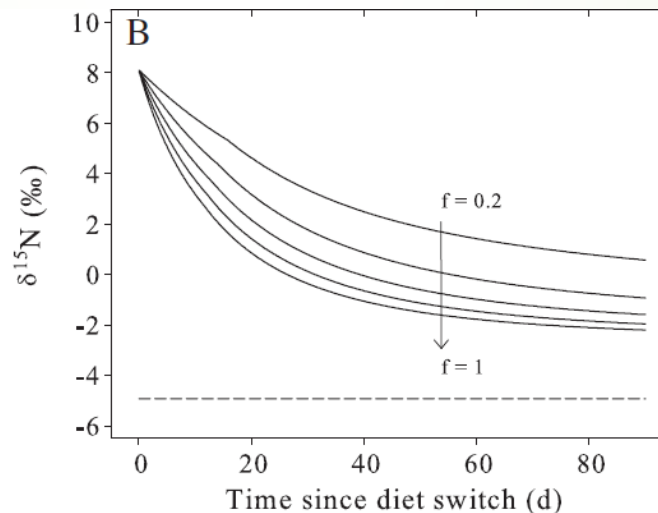
Laure Pecquerie, Roger M. Nisbet, Ronan Fablet, Anne Lorrain and Sebastiaan A. L. M. Kooijman



2011

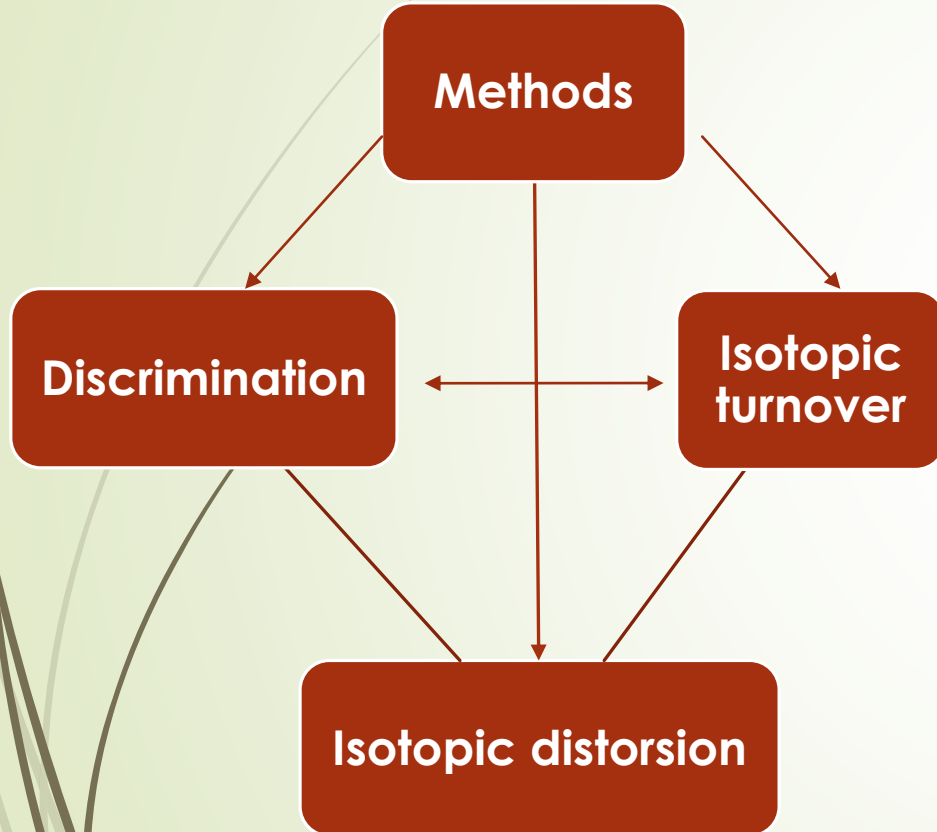
Understanding the dynamics of $\delta^{13}\text{C}$ and $\delta^{15}\text{N}$ in soft tissues of the bivalve *Crassostrea gigas* facing environmental fluctuations in the context of Dynamic Energy Budgets (DEB)

A. Emmery ^{a,b,c,*}, S. Lefebvre ^c, M. Alunno-Bruscia ^a, S.A.L.M. Kooijman ^d



Aims

- Large number of factors and complexities of their interactions
- DIB mechanistic modelling is a comprehensive framework
- Portability of DIB in community applications is questionable (also populations in some extent?)
- Aim: developing a more simple model that can be parametrised with DEB theory

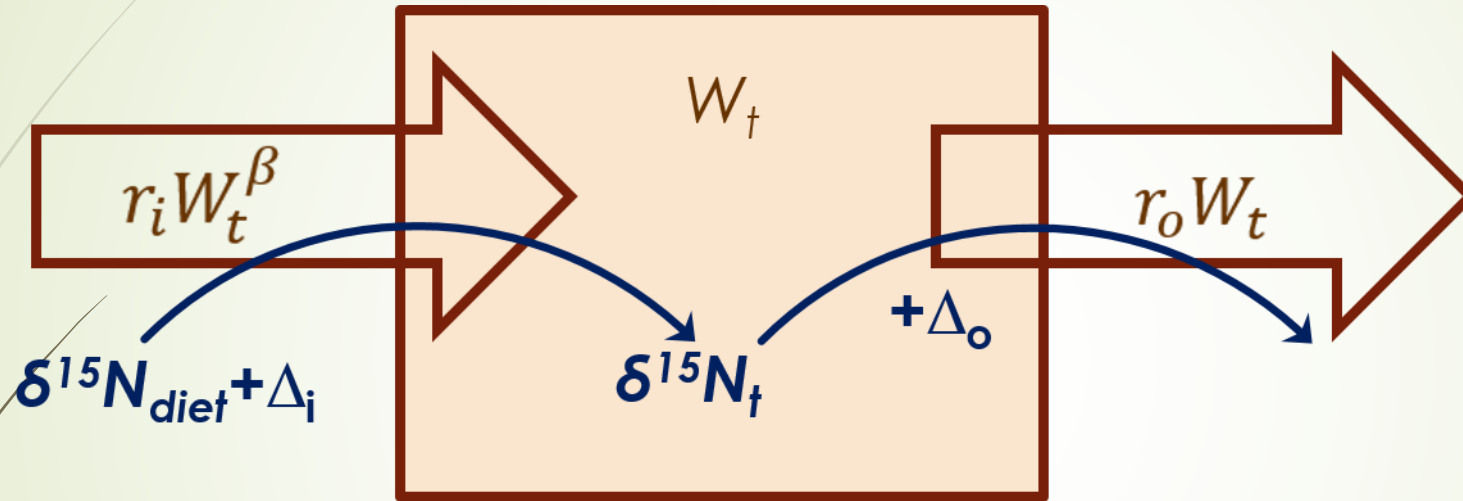


Coming out the fog....



IsoDyn model (a new model)

Nitrogen mass balance model



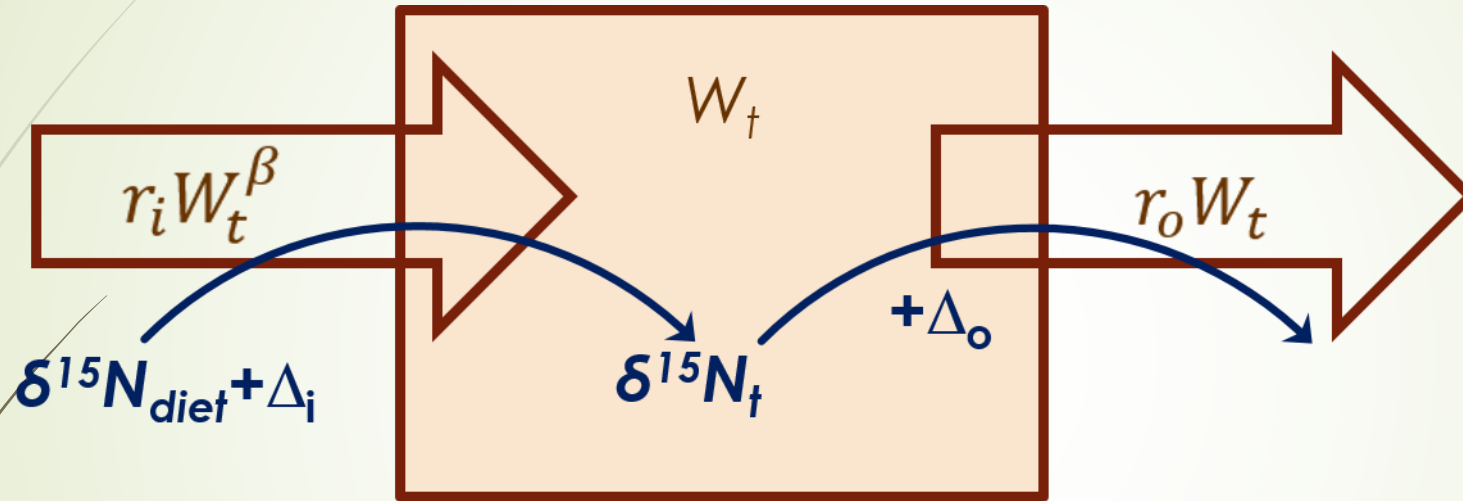
New features:

- Allometric growth (β)
- Two fractionations
- 4 parameters



IsoDyn model

Nitrogen mass balance model



New features:

- Allometric growth (β)
- Two fractionations
- 4 parameters

Determinate growth: $0.5 < \beta < 1$

For $2/3$ then Von Bertalanffy as explained by DEB theory

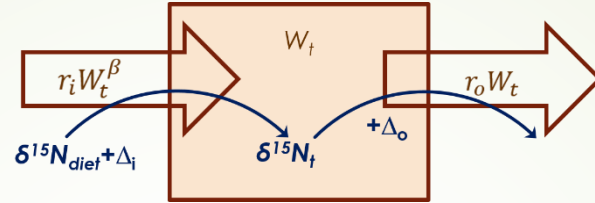
A system of two equations

$$W_t = \left\{ W_\infty^{1/3} + \left(W_0^{1/3} - W_\infty^{1/3} \right) e^{-\frac{r_0}{3} t} \right\}^3 \quad W_\infty^{1/3} = \frac{r_i}{r_o}$$

$$\frac{d\delta^{15}N}{dt} = r_i W_t^{1-\beta} (\delta^{15}N_{diet} - \delta^{15}N + \Delta_i) - \Delta_o$$



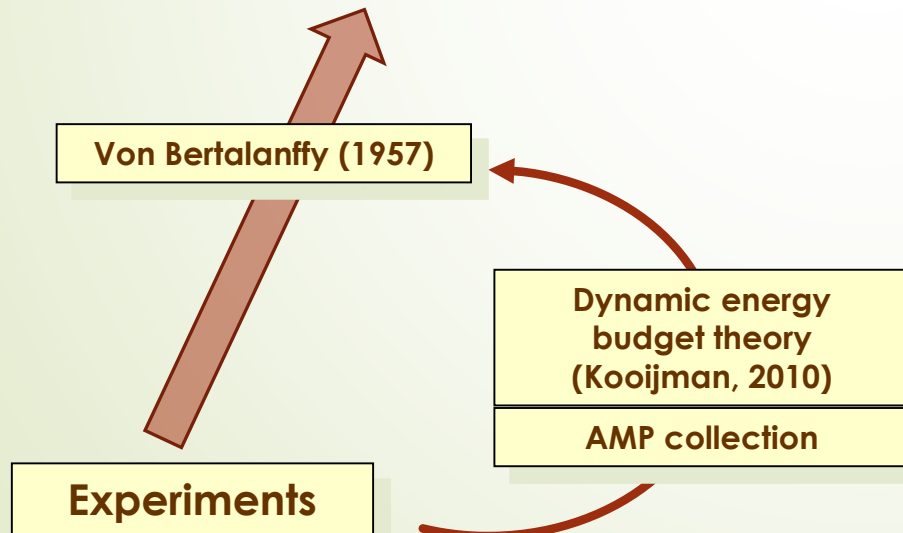
How to calibrate IsoDyn from DEB?



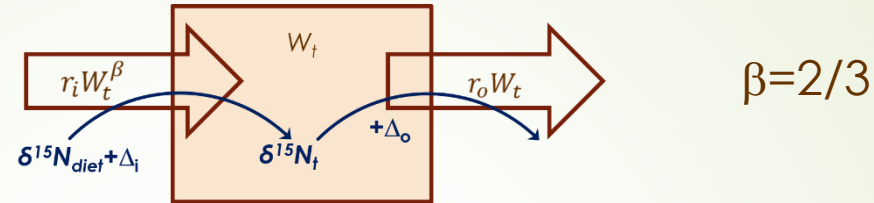
$$\beta = 2/3$$

Two-step process

Anabolic and catabolic parameters: r_i and r_o



How to calibrate IsoDyn from DEB?



Two-step process

1 Anabolic and catabolic parameters: r_i and r_o **INDEPENDENT** Fract. Δ_i and Δ_o

New

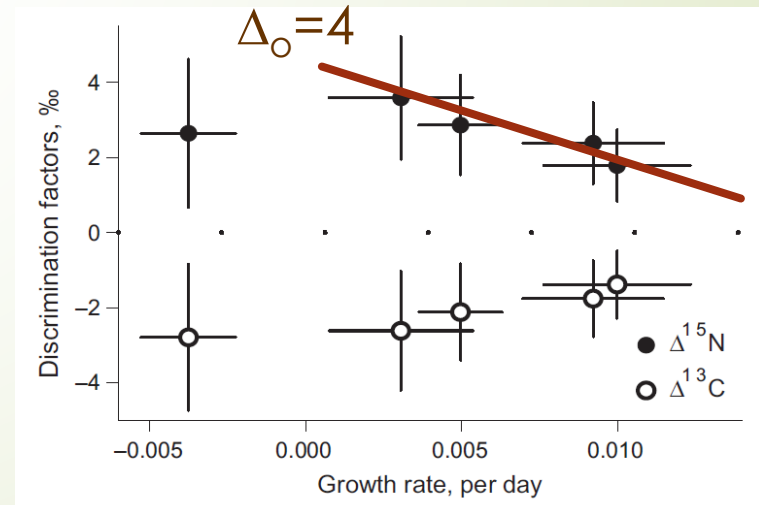
Diet switch experiments
At several growth rates with comparable diets or species

Von Bertalanffy (1957)

Dynamic energy budget theory
(Kooijman, 2010)

AMP collection

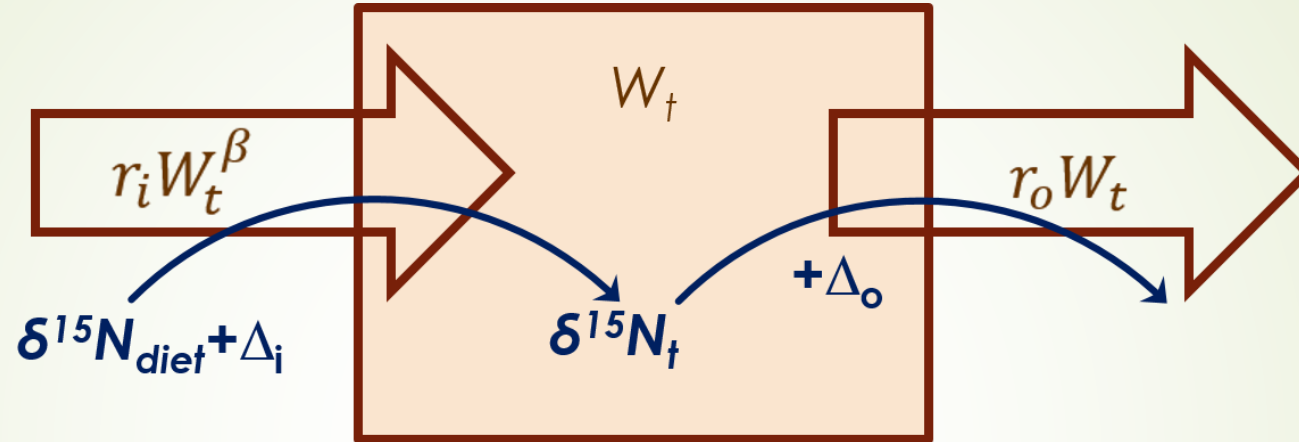
Experiments



Mysids
Gorokhova 2017



How to calibrate IsoDyn from DEB?



5 DEB parameters
+Temp correction

« Anabolic » parameter

$$r_i = \frac{k_M}{f + g} W_i^{\frac{1}{3}}$$

Infinite weight

$$W_i = (f s_M L m)^3 (1 + f w)$$

« Catabolic » parameter

$$r_o = \frac{k_M}{f + g}$$

Isotopic turnover (λ)

$$\lambda = \frac{k_M}{f + g} W^{-\frac{1}{3}} W_i^{\frac{1}{3}}$$

Discrimination (Δ)

$$\Delta = \Delta_i + \Delta_o \frac{r_o}{\lambda}$$



Example: *Neomysis integer* (Opossum shrimp)

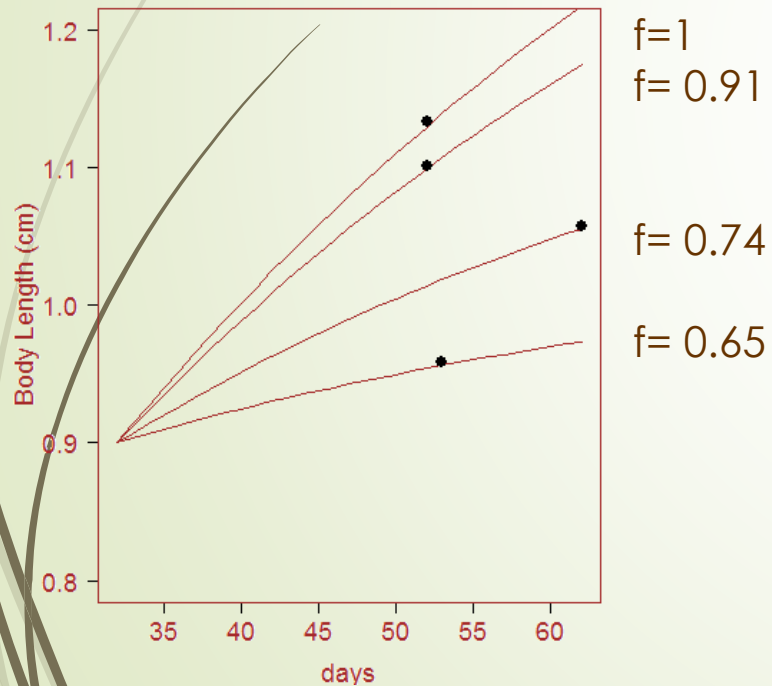


Data from Gorokhova 2018

An experiment with several food levels and isotopic incorporation dynamics

Parameters from AMP (abj model)

Adj functional scaled response



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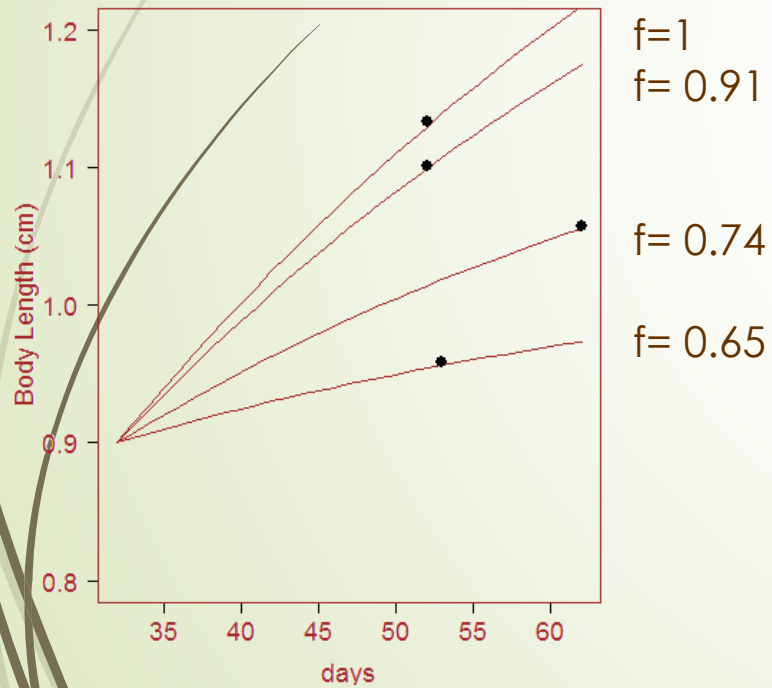


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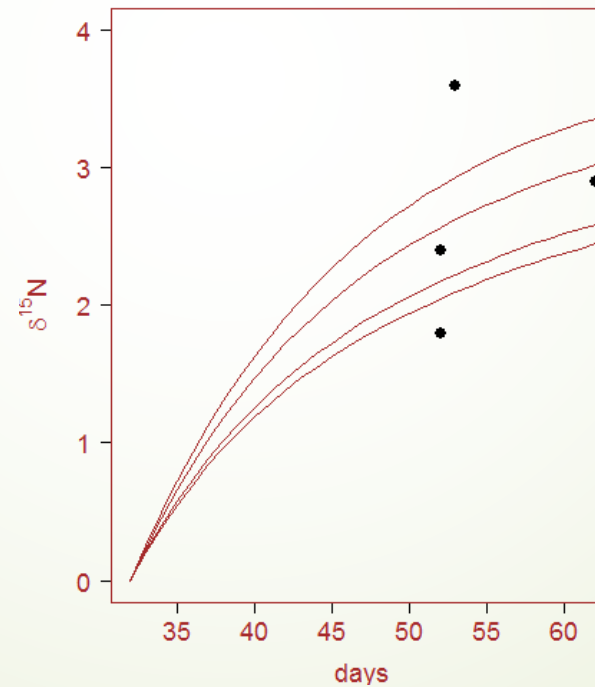
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$\delta^{15}\text{N}$ dynamics



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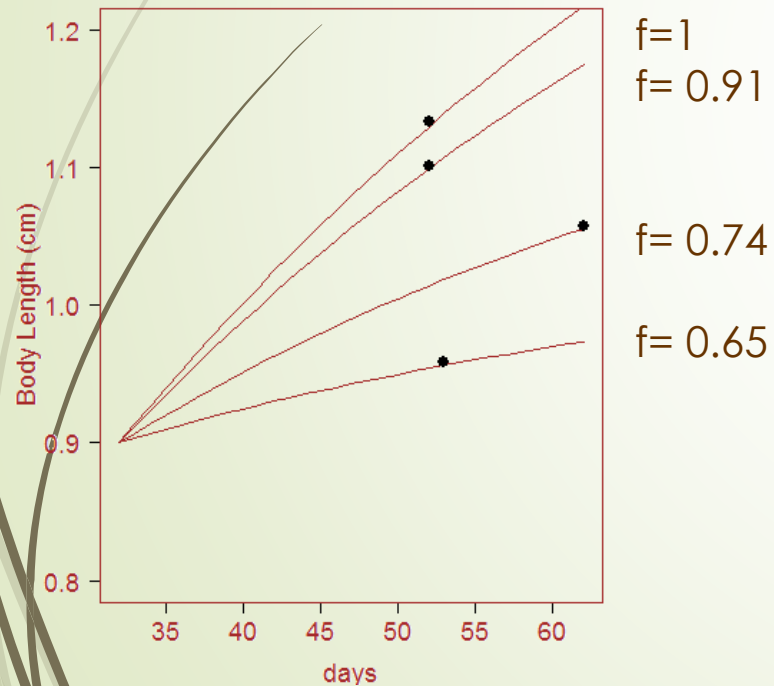


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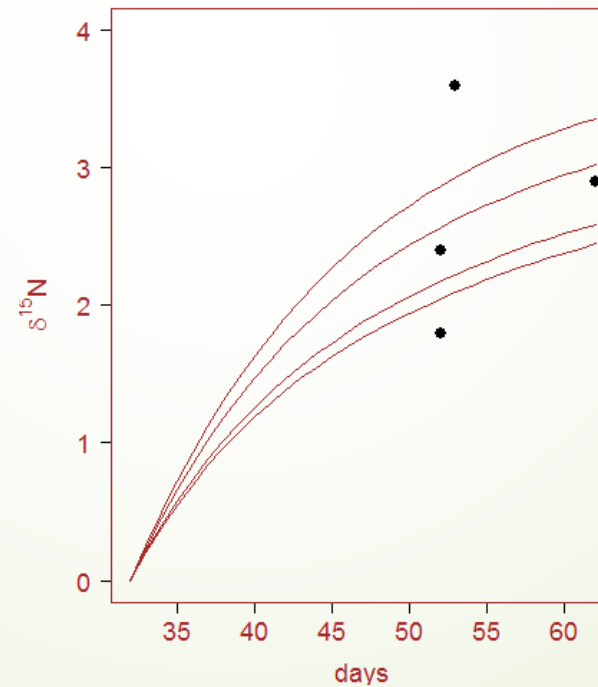
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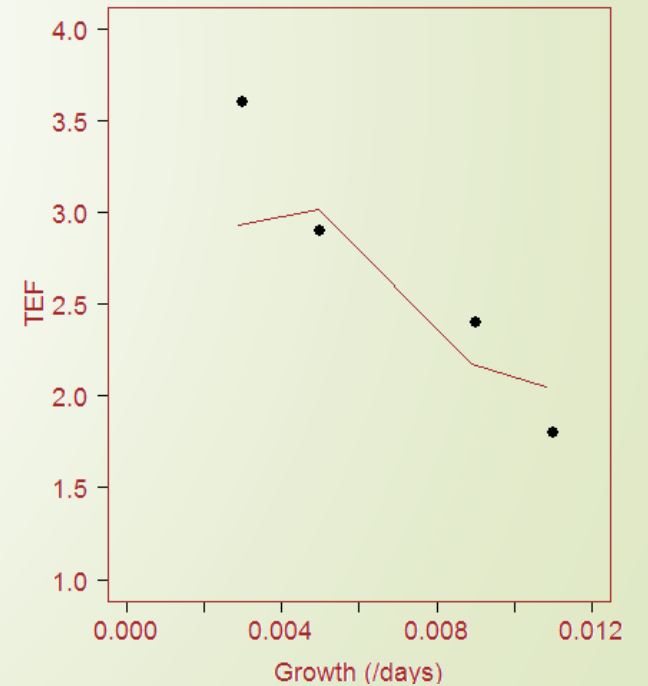
Adj functional scaled response



$\delta^{15}\text{N}$ dynamics



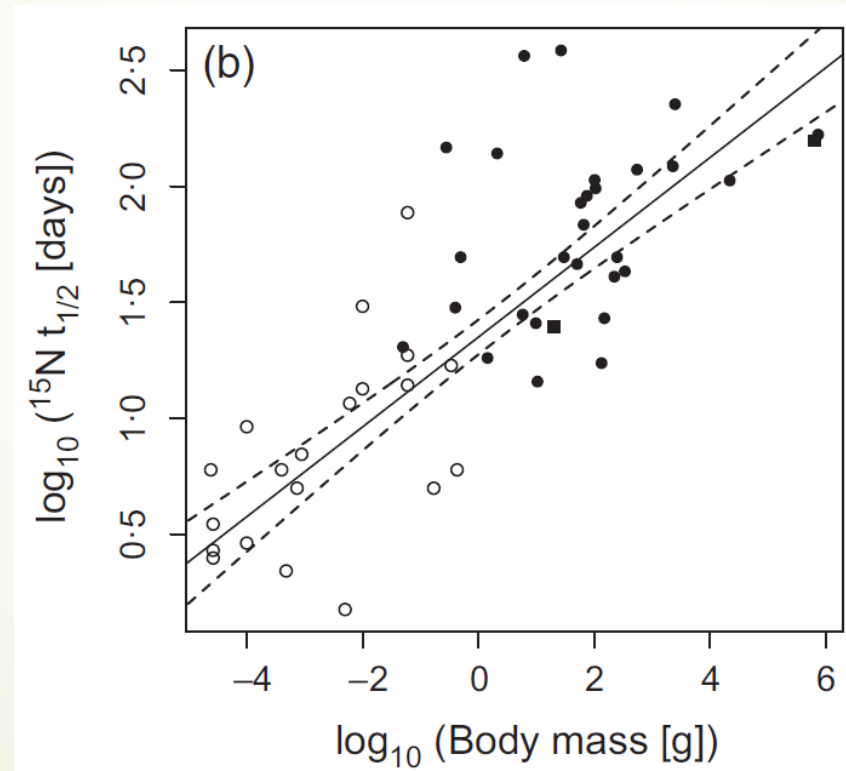
Δ vs growth rate



Isotopic half life (inverse of turnover rate)

$$t_{\frac{1}{2}} = \frac{\ln 2}{\lambda}$$

Isotopic Half-life vs body mass (Muscle)
→ Allometric rule (slope=0.19)



Each point one exp and one species

Ectotherms (empty circles)
Endotherms (full circles)



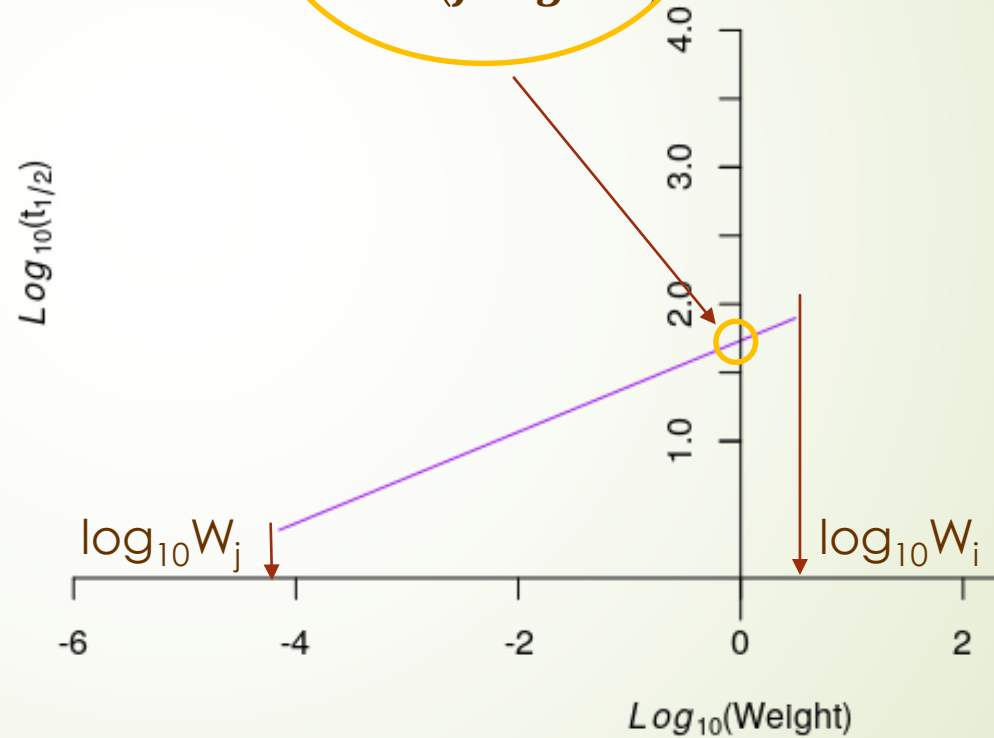
Isotopic half life (through IsoDyn and DEB)

$$t_{\frac{1}{2}} = \frac{\ln 2}{\lambda}$$



Sand goby

$$\log_{10} \left(t_{\frac{1}{2}} \right) = \log_{10} \left(\frac{\ln 2}{\frac{k_M}{f+g} W_i^{\frac{1}{3}}} \right) + \frac{1}{3} \log_{10} W$$



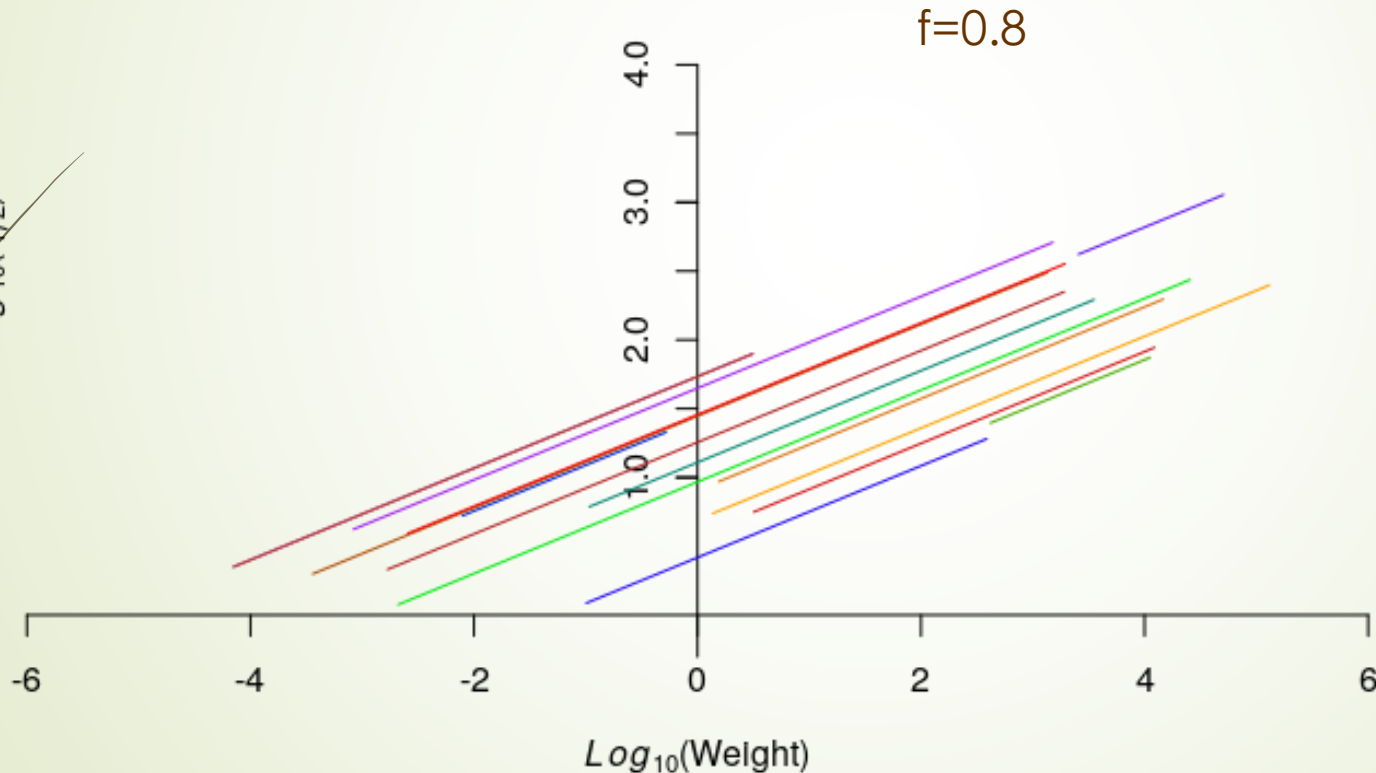
f=0.8



Isotopic half life (through IsoDyn and DEB)

$$t_{\frac{1}{2}} = \frac{\ln 2}{\lambda}$$

$\text{Log}_{10}(t_{1/2})$

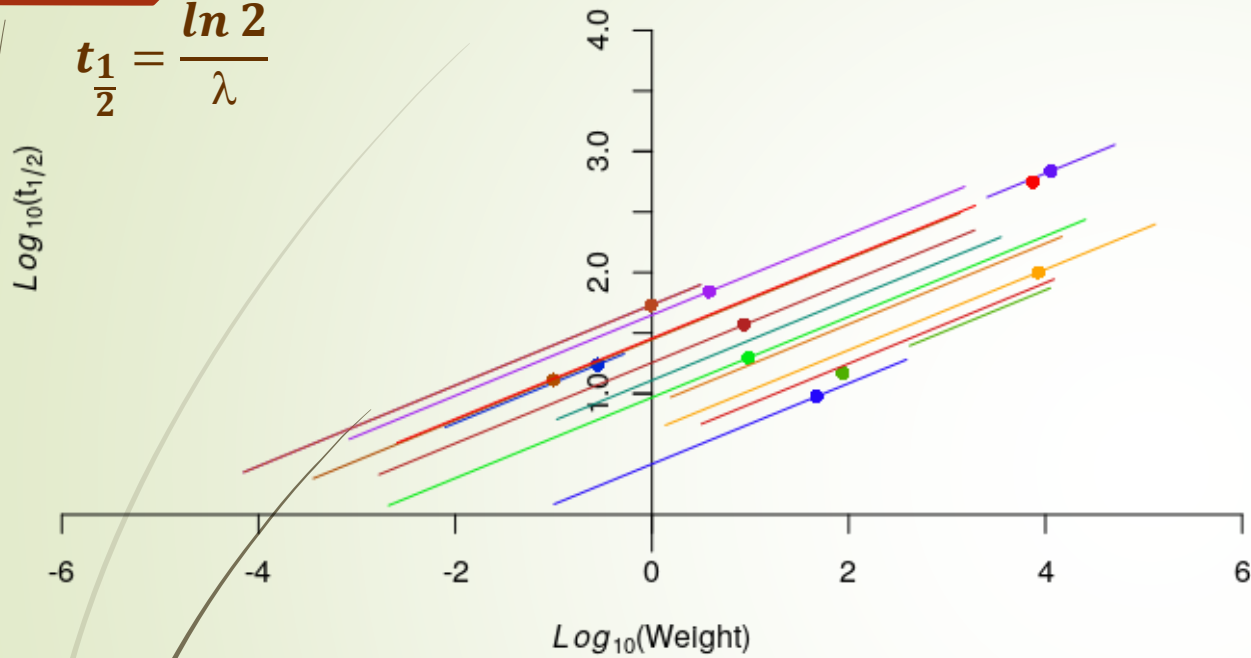


- Barbus_barbus
- Carcharhinus_plumbeus
- Clupea_pallasii
- Danio_rerio
- Dicentrarchus_labrax
- Gadus_morhua
- Ictalurus_punctatus
- Mugil_liza
- Mycteroperca_microlepis
- Oncorhynchus_mykiss
- Oreochromis_niloticus
- Pomatoschistus_minutus
- Salvelinus_namaycush
- Thunnus_orientalis

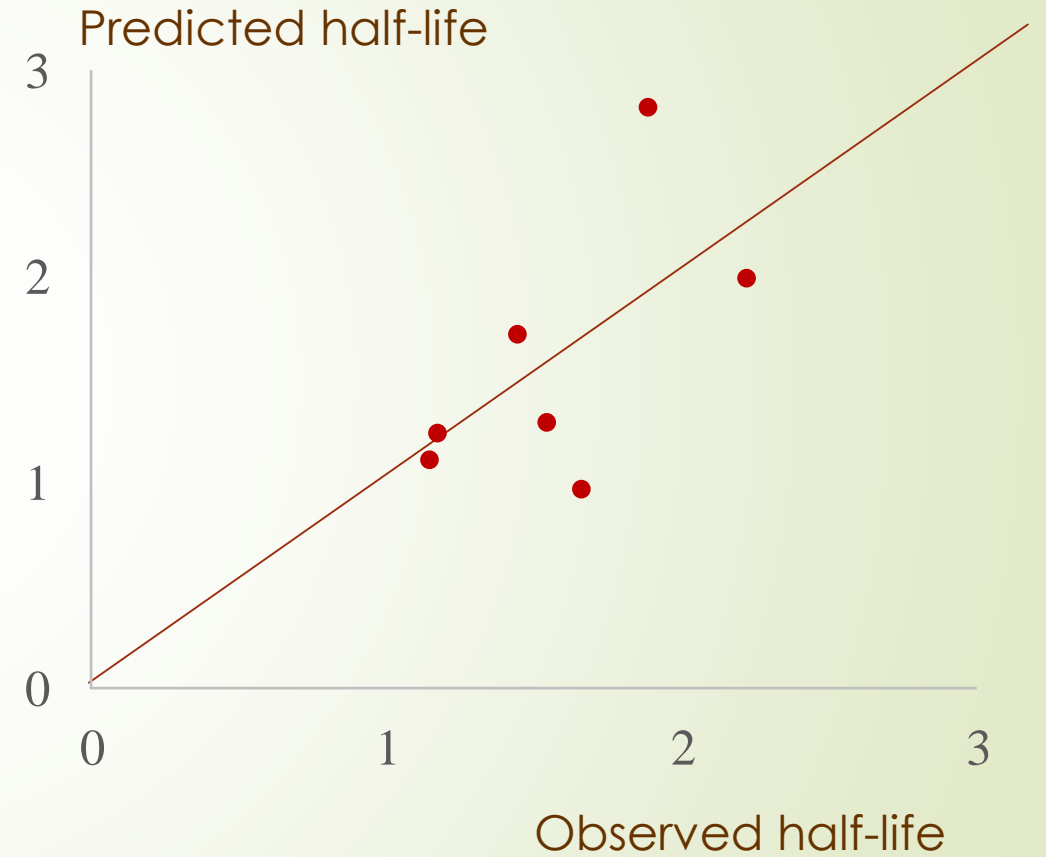


Isotopic half life (through IsoDyn and DEB)

$$t_{\frac{1}{2}} = \frac{\ln 2}{\lambda}$$

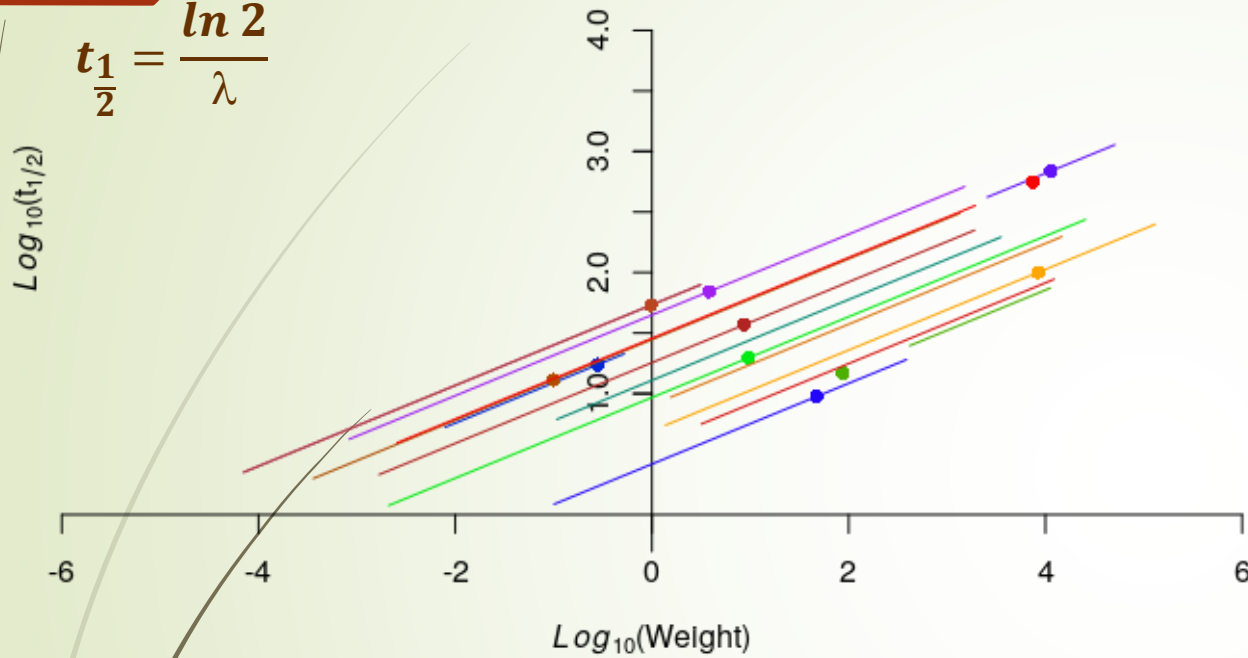


f=0.8 (not adjusted)

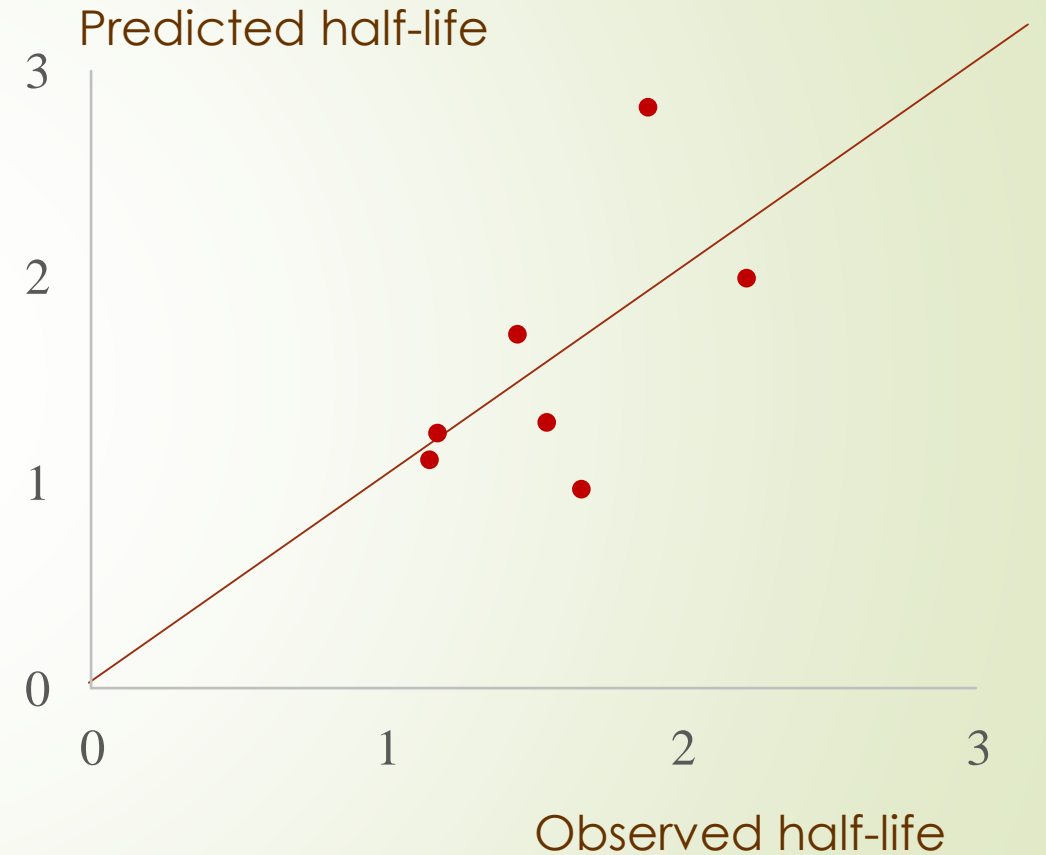


Isotopic half life (through IsoDyn and DEB)

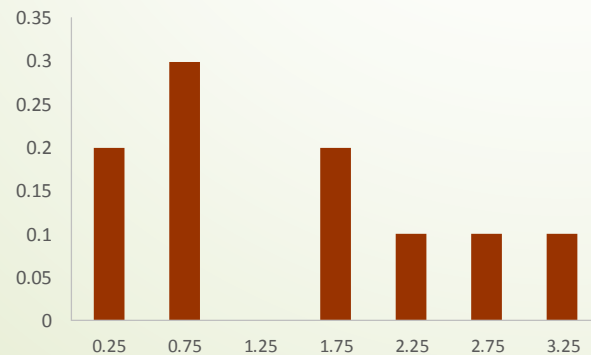
$$t_{1/2} = \frac{\ln 2}{\lambda}$$



f=0.8 (not adjusted)



Freq of Discrimination

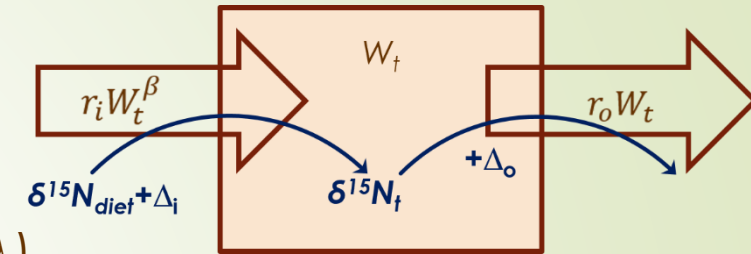


$$\Delta = \Delta_i + \Delta_o \frac{r_o}{\lambda}$$



Take home messages

- New model with allometry rules and two fractionations (in and out)
- All dynamics:
Discrimination (Δ) + incorporation rate (λ) + their interactions ($\Delta \cap \lambda$)
- Portability is high

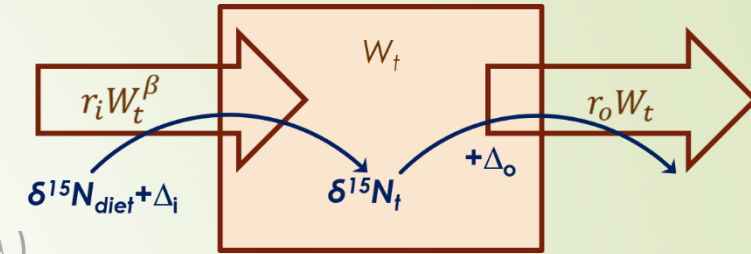


Take home messages

- New model with allometry rules and two fractionations (in and out)
- All dynamics:
Discrimination (Δ) + incorporation rate (λ) + their interactions ($\Delta \cap \lambda$)
- Portability is high

Future directions

- Continue to re-interpret meta-analysis results (Δ and λ) using DEB through IsoDyn
- Add isotope dynamics in AMP (add my « iso »Pet)
- Produce R packages with links to AMP collection
- Using DIB as a reference to Isodyn (comparison)
- Most experimental studies done on tissues not on whole body...need for an extension of the DIB model (several structures)
- Isotopic routing (several reserves)



Join the team ! (Post-doc position offer http://log.cnrs.fr/Post-Doc-Position-ISIT_U)



Thanks

Thanks for your attention



Sébastien Lefebvre,



Marine Ballutaud,



Carlos Martinez Del Rio,



Laure Pecquerie

Thanks to DEB2019 organizing committee



Debbie the special guest

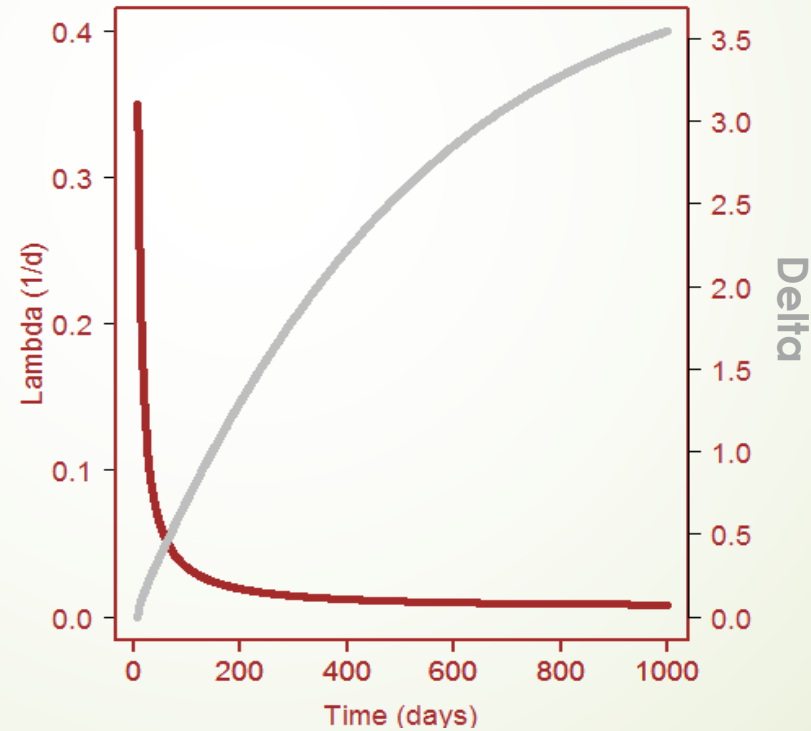
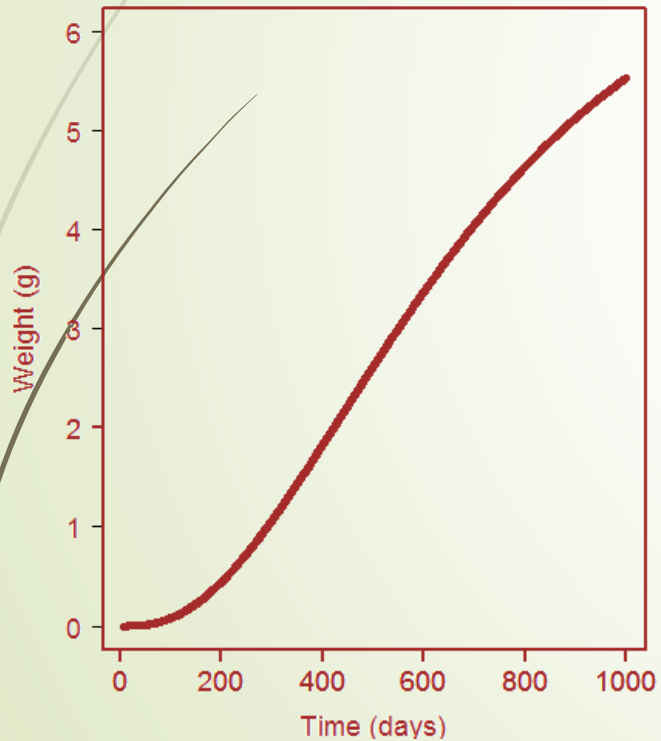
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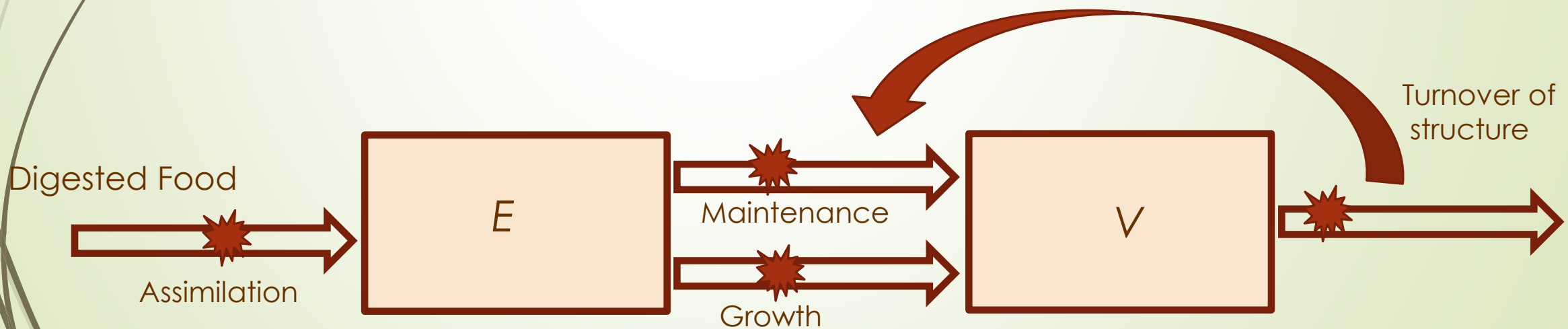
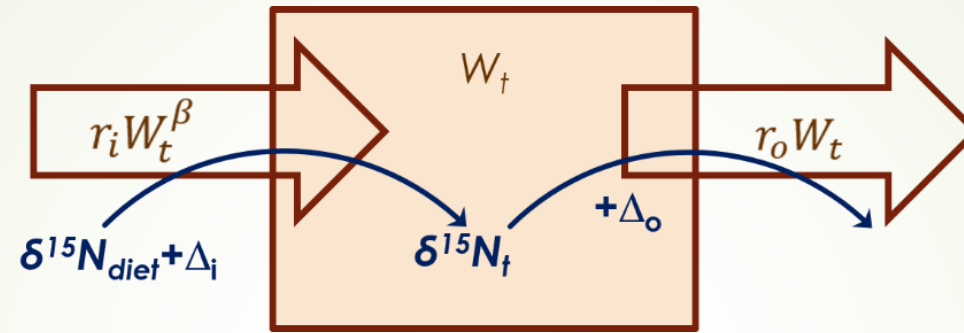
Example: *Pomatoschistus minutus* (Sand goby)



Parameters from AMP (std model)



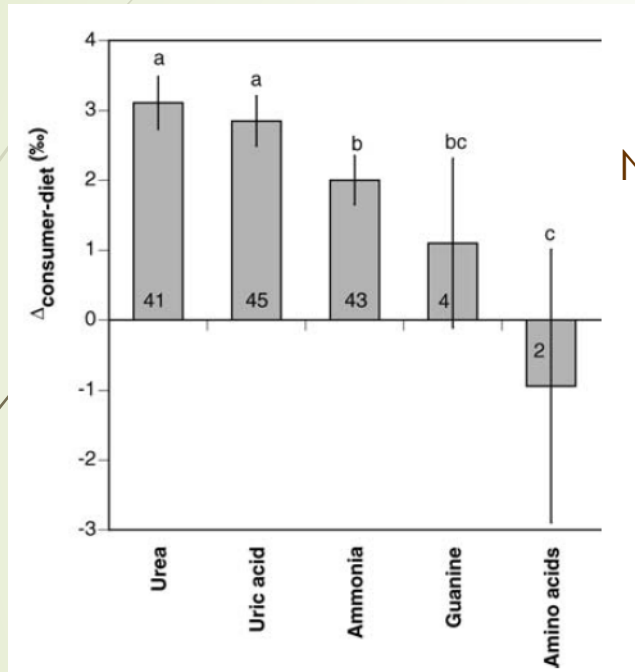
Comparing IsoDyn (DEB) with DIB



Sources of isotopic anamorphosis: Δ

Discrimination factor (or TEF or trophic fractionation...)

- Quite numerous and descriptive values but **few mechanistic rules**



Nitrogen excretion types

Discrimination

Methods
DSE

Isotopic
turnover

Isotopic
anamorphosis

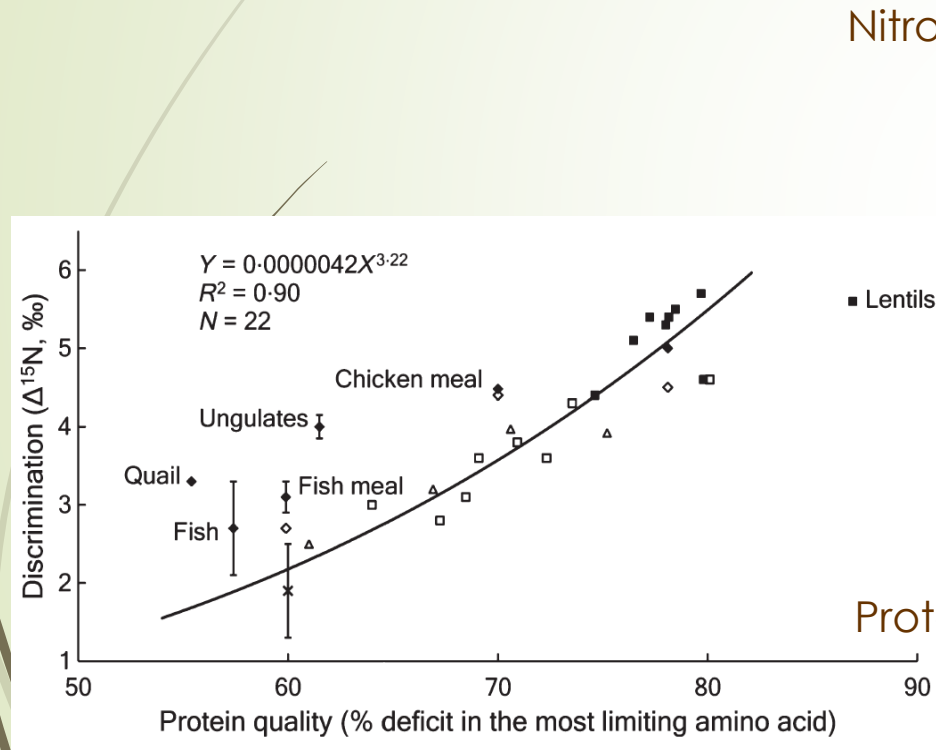
Vanderklift and
Ponsard, 2003



Sources of isotopic anamorphosis: Δ

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Nitrogen excretion types

Protein quality and quantity

Discrimination

Methods
DSE

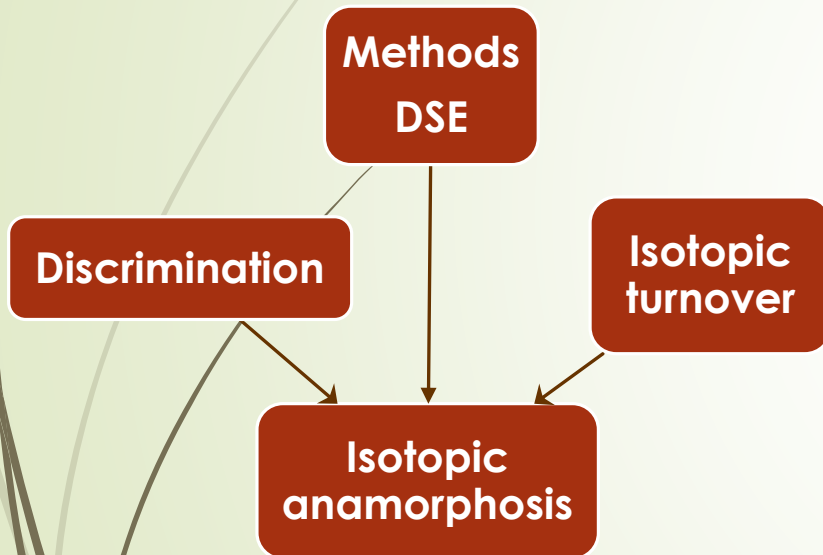
Isotopic
turnover

Isotopic
anamorphosis

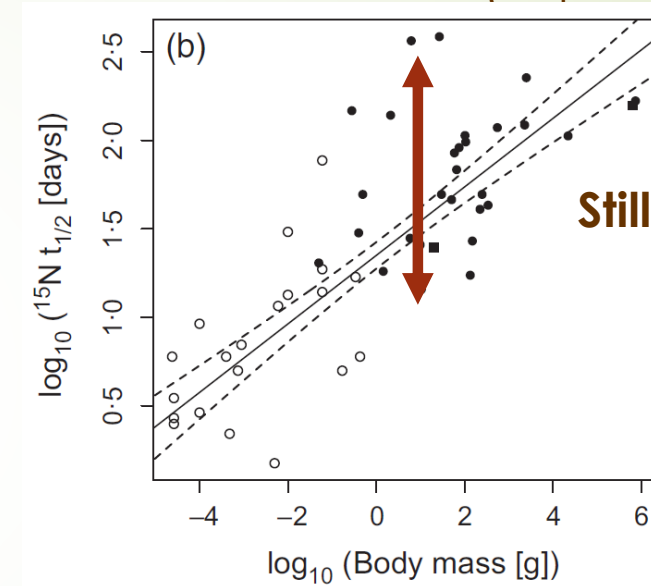


Sources of isotopic anamorphosis: λ

Isotopic turnover rate



Isotopic Half-life vs body mass (Muscle)
→ Allometric rule (slope=0.19)



Thomas and Crowther, 2015

Growth
Nutritional status
Experimental conditions
Species
Life stage....

Vander Zanden et al., 2015



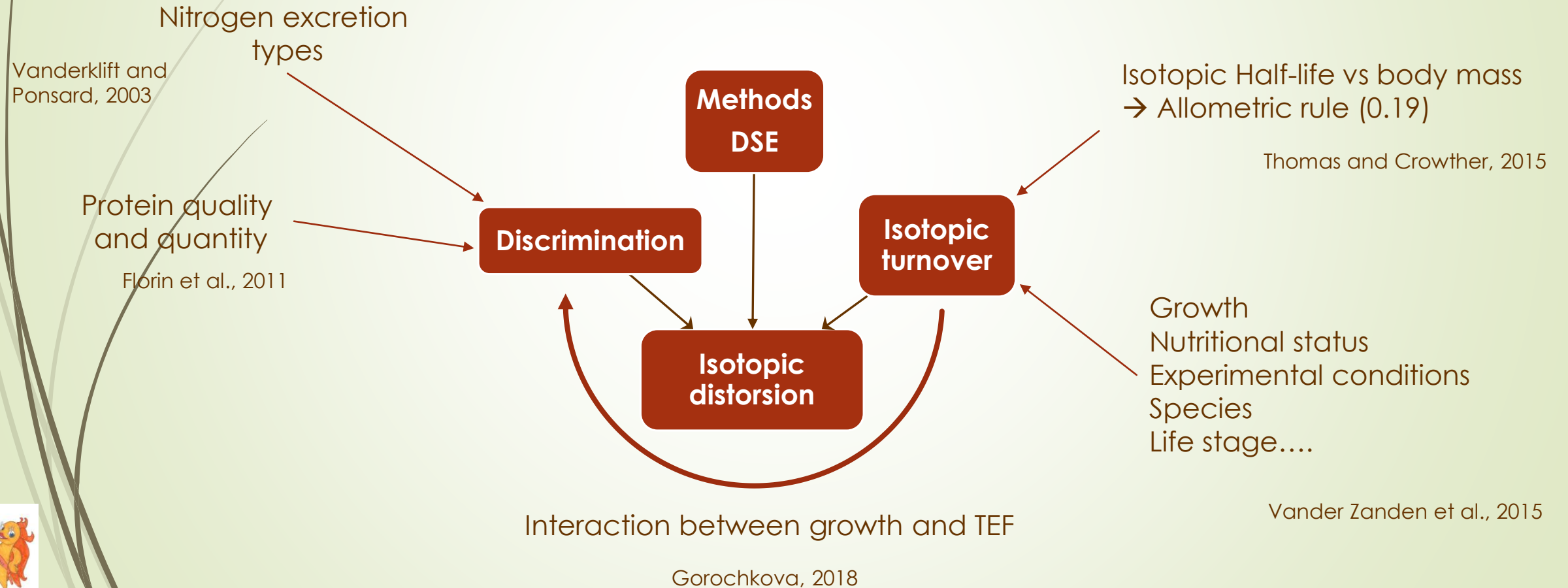
Sources of isotopic distortion: Δ and λ

Discrimination factor

and

Isotopic turnover rate

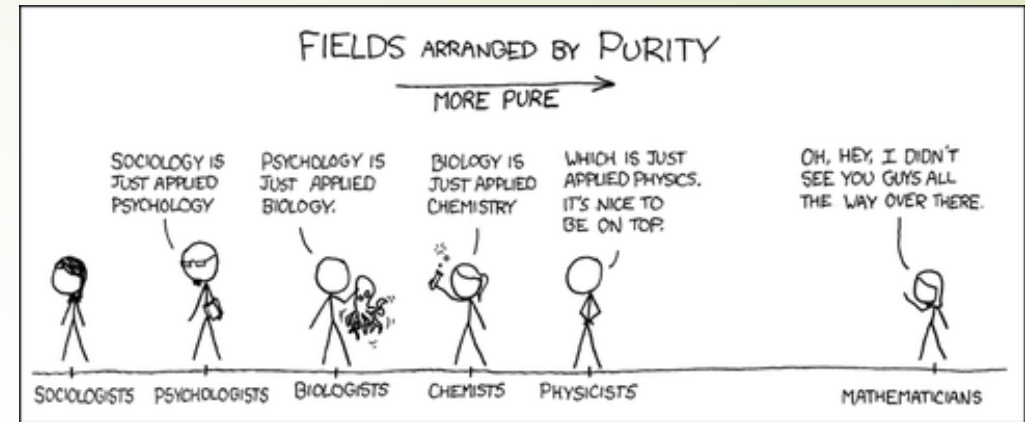
- Quite numerous and descriptive values but **few mechanistic rules**



$$t_{\frac{1}{2}} = \frac{\ln 2}{\lambda} = \frac{\ln 2}{\frac{k_M}{f+g} W_i^{\frac{1}{3}}} W^{\frac{1}{3}}$$



Existing models



Empirical
2-3 parameters

Hesslein et al. (1993)

Carleton & Martinez Del Rio (2010)

1 compartment
Growth steady state
4-5 parameters
No explicit bioenergetics

Olive et al. (2003)

Ponsard and Averbuch (1999)

Martinez del Rio and Wolf (2005)

IsoDyn

1 compartment
4 parameters

Lefebvre et al. (2019?)

Dynamic isotopic budget
DEB theory

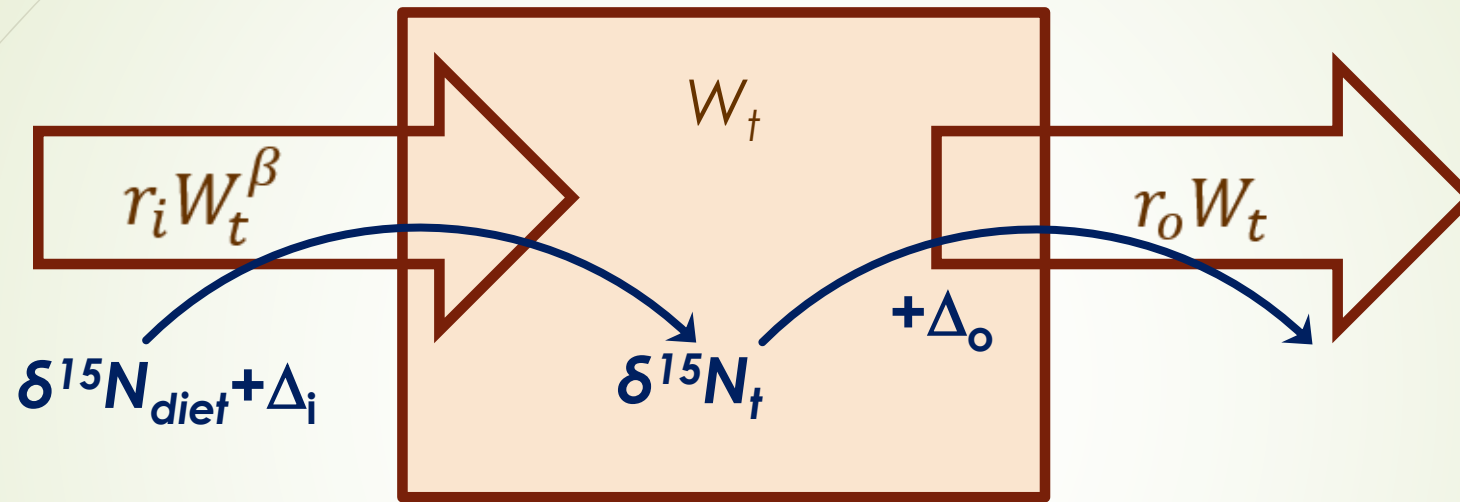
3 compartments
15 parameters
Zoo of 1000 species

Pecquerie et al. (2010)

Phenomenological

Mechanistic





$$\left. \begin{aligned}
 W_t &= \left\{ W_\infty^{1-\beta} + (W_0^{1-\beta} - W_\infty^{1-\beta}) e^{-r_o(1-\beta)t} \right\}^{\frac{1}{1-\beta}} & W_\infty^{1-\beta} &= \frac{r_i}{r_o} \\
 \frac{d\delta^{15}N}{dt} &= r_i W_t^{1-\beta} (\delta^{15}N_{diet} - \delta^{15}N + \Delta_i) - \Delta_o
 \end{aligned} \right\}$$

